



Thermal control in building using MPC under air quality constraints

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- 40% of energy consumed by buildings worldwide
 - Strategies for
 - Energy conservation
 - Energy savings
 - Better coordination among Building Automation Systems (FP7 SCUBA project)
-
- One of TOPAs objectives: **advanced control techniques**
 - Ventilation
 - Heating
- Energy savings
- Take into account “user comfort”, at least bounds on Temp. & CO2



Objectives

- **Develop a generic (D)MPC framework to support control design**
- **Deploy, Test and Validate**
 - Post-grad room in NIMBUS
 - Improve thermal comfort and air quality
 - Energy savings
 - Peak demand management / energy cost
- **Post-grad room : open office in NIMBUS building**
 - CIT Campus, Cork, Ireland
 - Climate zone : temperate maritime (mild winter, cool summer, regular rains)



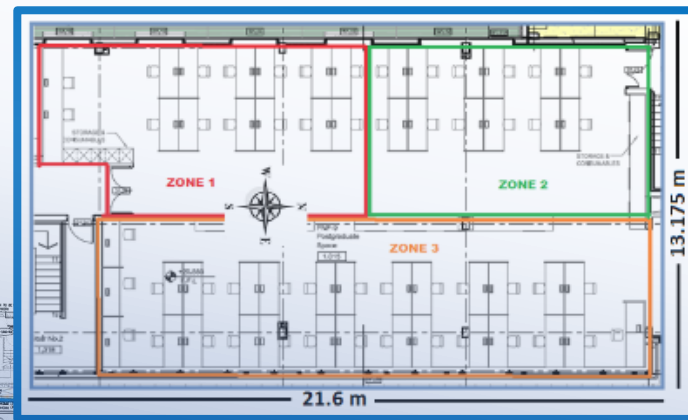
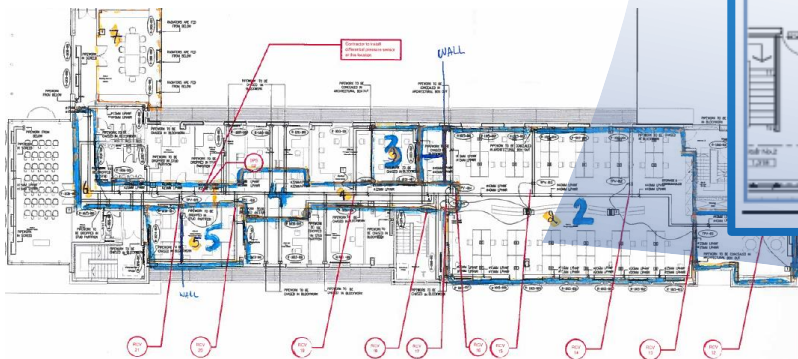


- Context and objectives
- “System” under study
- Modelling
 - Thermal: white-box lumped capacitance (2RC)
 - CO₂ concentration: mass balance
- Model Predictive Control for thermal and CO₂ regulation
- Implementation in real field
 - Model tuning with real field data
 - Modelling for control?
- Next steps



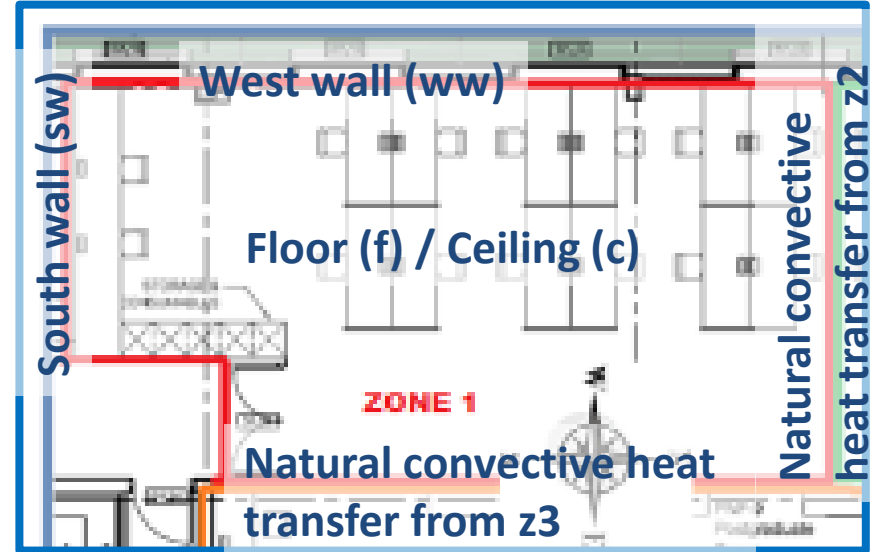
“System” under study

- NIMBUS – Proof of Concept
 - Post-grad area split in 3 zones
 - White box model
 - CO2 concentration, thermal RC equivalent model
 - Coupling between zones (CO2 and temp.)
 - Natural ventilation, controlled openings (windows)
 - Outdoor conditions
 - Modular → “extendable”

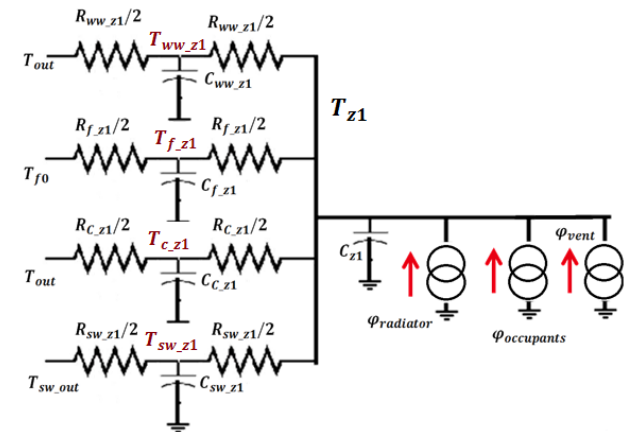


3 virtual zones
single space

- For each zone:
Simplified Lumped capacitance model (2RC)
 - Coupling** between zones (natural convective heat transfer)
 - Influence of **#occupants** ϕ
 - Influence of heaters (r)
 - Influence of **openings** (natural leak, windows opening) (outdoor temperature)
 - For zone 1: 6 ODEs:
 $T_1, T_{sw}, T_{ww}, T_f, T_c, T_r$
 - Similar approach for other zones



Continuous
time non-
linear model

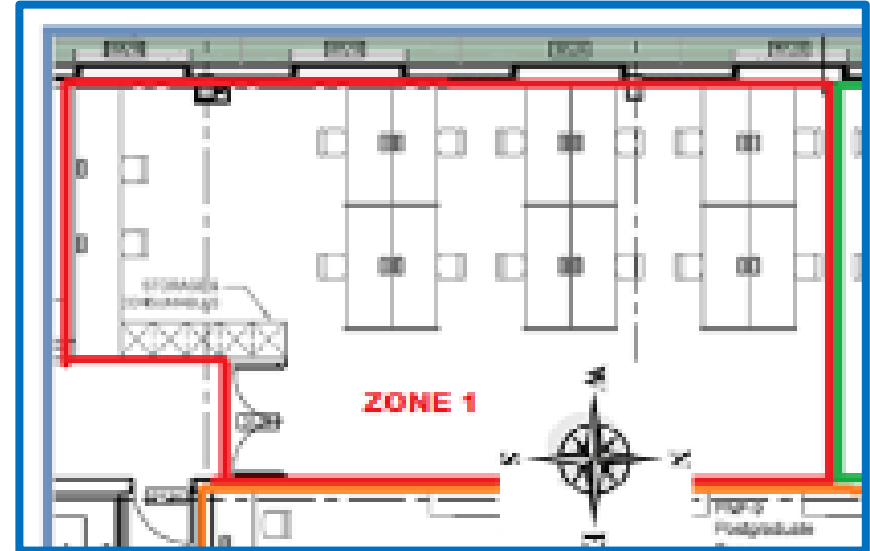


- For each zone:

Mass balance

- **Coupling** between zone (diffusion via Fick's law)
- Influence of **openings** (natural leak, windows opening) (outdoor CO₂)
- Influence of **#occupants**
 - Uniform distribution over the room
- 1 ODE per zone

Continuous time linear model



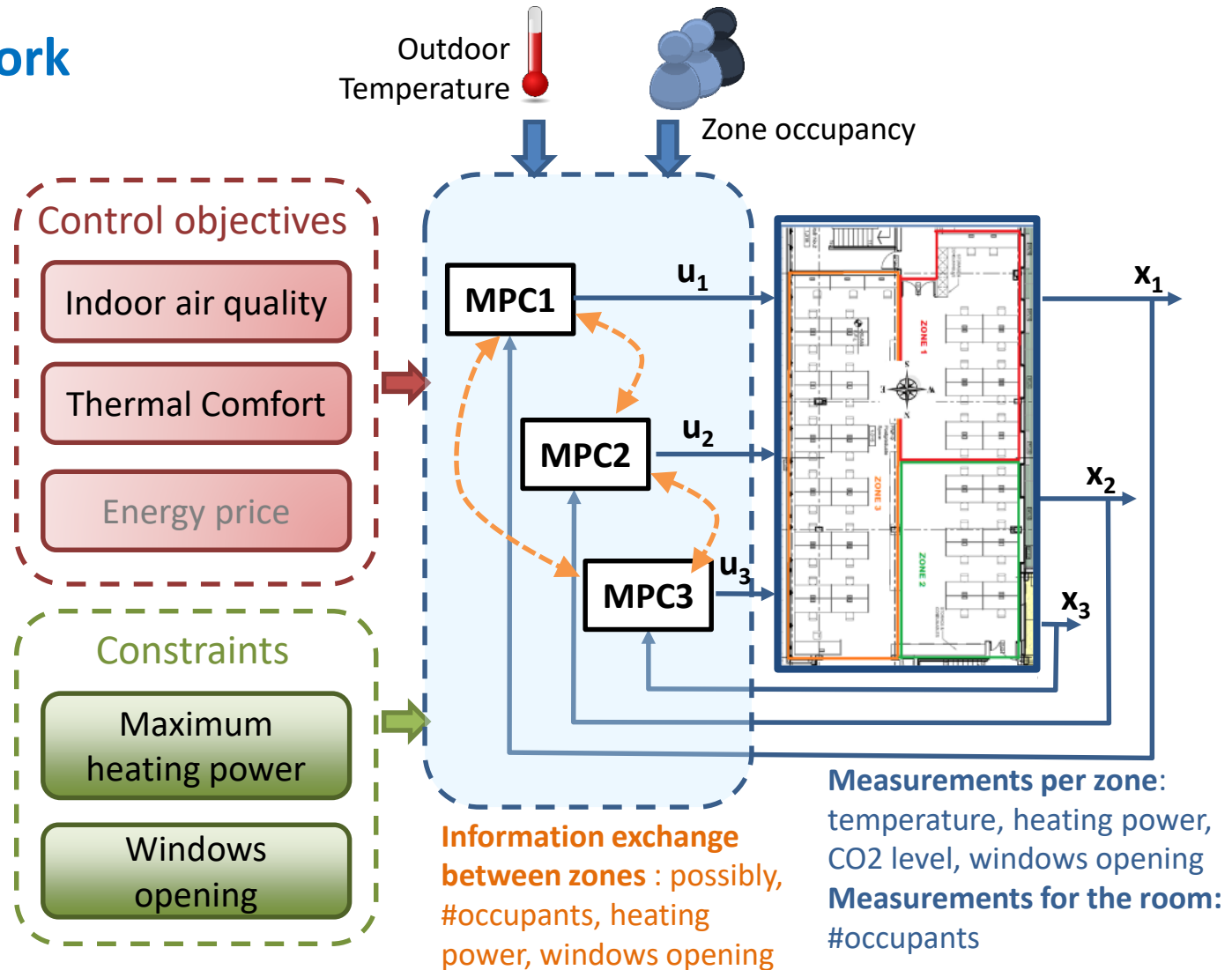
For both parts of the model:
parameters fixed thanks to **basic knowledge** on building materials, building geometry, mean CO₂ production and heat per occupant



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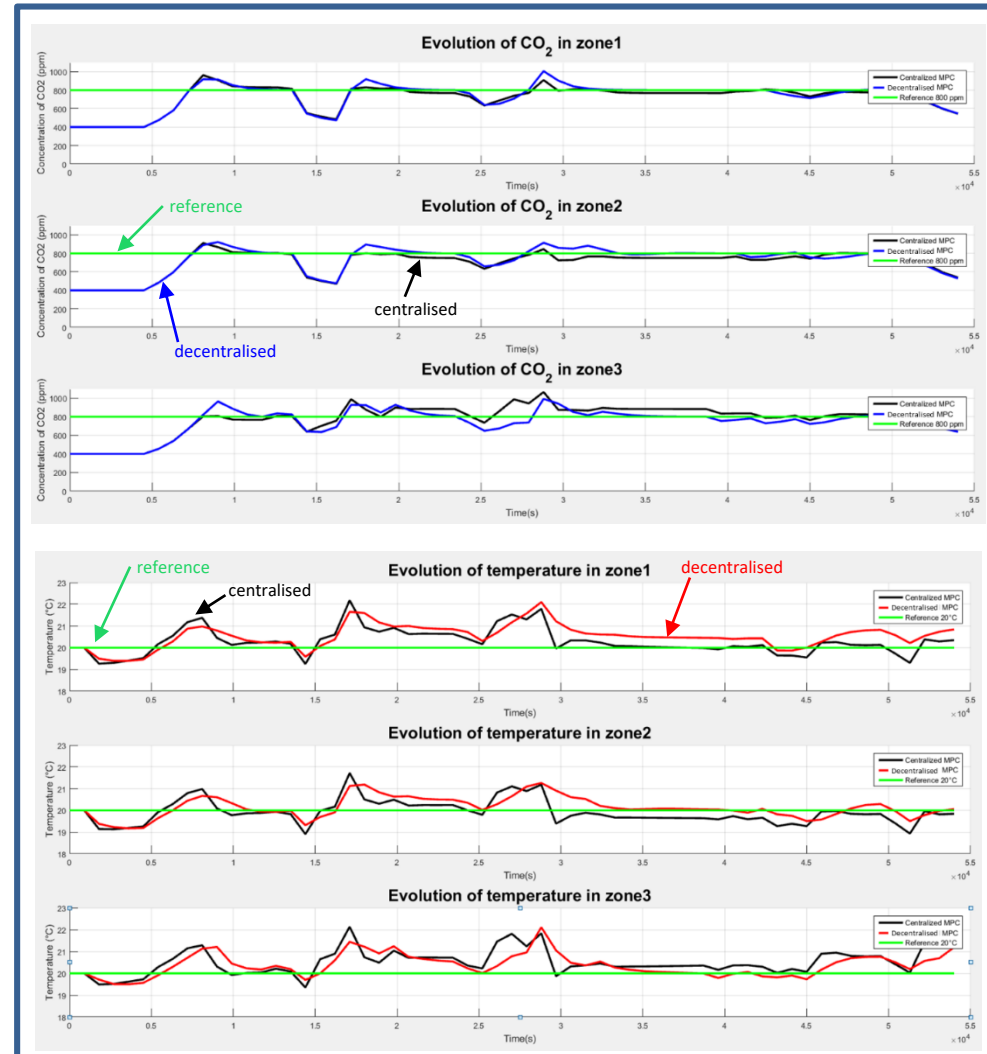
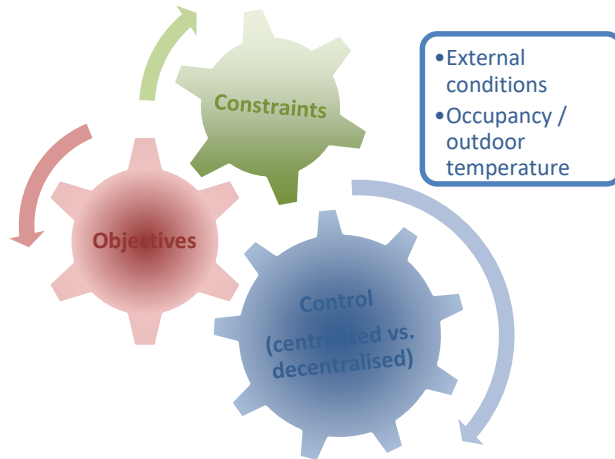
(D)MPC framework



$$J = \sum_{j=1}^N \left\{ \underbrace{\|(y - y_{ref})(k+j)\|_Q^2}_{\text{Comfort}} + \underbrace{\|\Delta u(k+j)\|_R^2}_{\text{Energy}} \right\}$$



Results in simulation



Power Consumption (kWh)	Conventional Control (on/off)	Centralized Control (CMPC)	Decentralized Control (DeMPC)
Total	181	127,83	138,59
Gain compared with conventional controller	0%	30%	23,5%

	Number of states	Number of inequalities /equalities	Average optimi. time per sampling time (normalized)
CPMC	21	660	4.7
DeMPC	7	220	1



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- Have a **realistic comportemental model**
 - Parameter identification $\hat{\theta}$ for model tuning
 - **Instead of R and C** , identify time constants $\tau = RC$
 - **Building geometry known**

- Non-linear optimisation pb with constraints (+ODE integration)

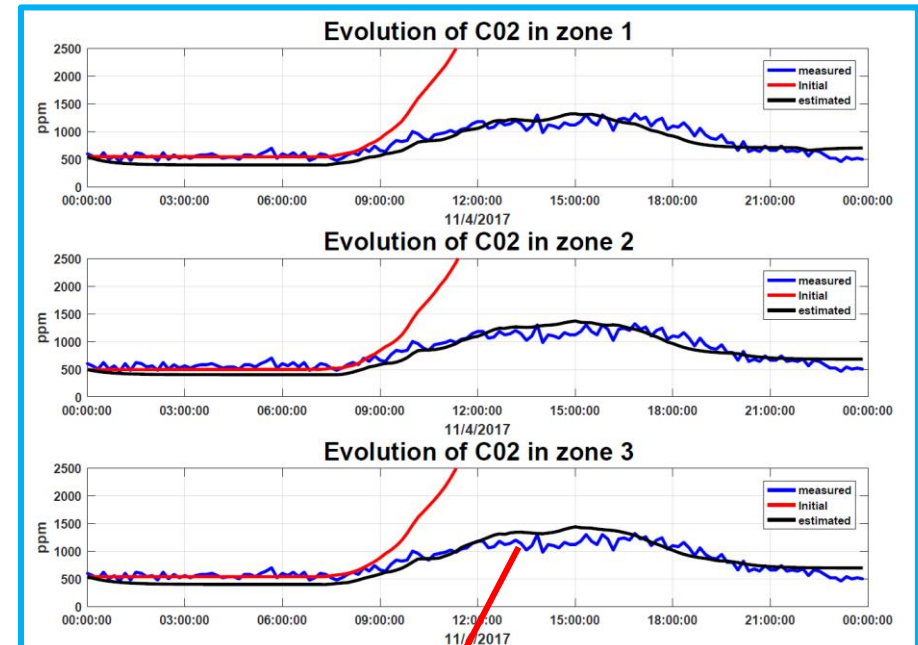
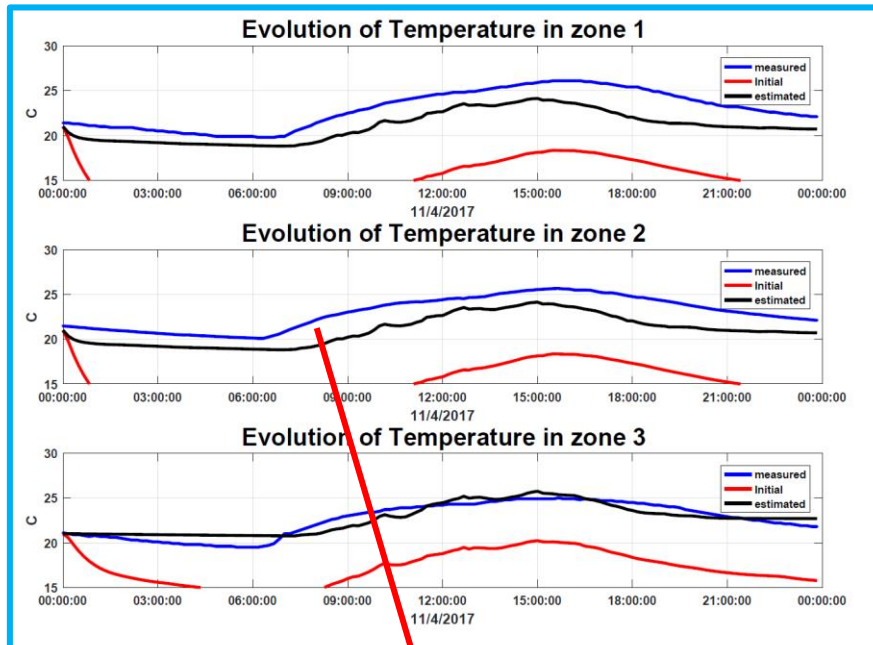
$$\hat{\theta} = \operatorname{argmin}\{\|x(t, \theta) - \text{measures}(t)\|_2^2\}$$

$$\text{s.t. } \theta \in [\theta_{\min}, \theta_{\max}]$$

$$\text{where } \frac{dx}{dt} = f(x, u, t, \theta)$$



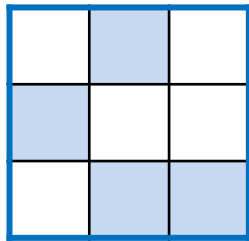
- Data extracted from TOPAs oBMS
- Parameter **identification** and model **validation** for the **white-box continuous-time non-linear model**



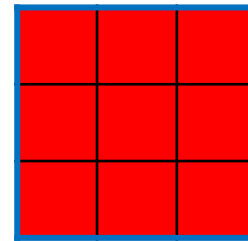
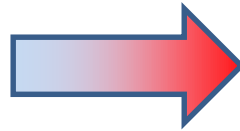
#occupants? Windows opening?

Initial model
Measurements
Model tuned

- White box model → state space model for MPC
 - Linearisation
 - Exact discretisation: matrix exponential



Sparse matrix



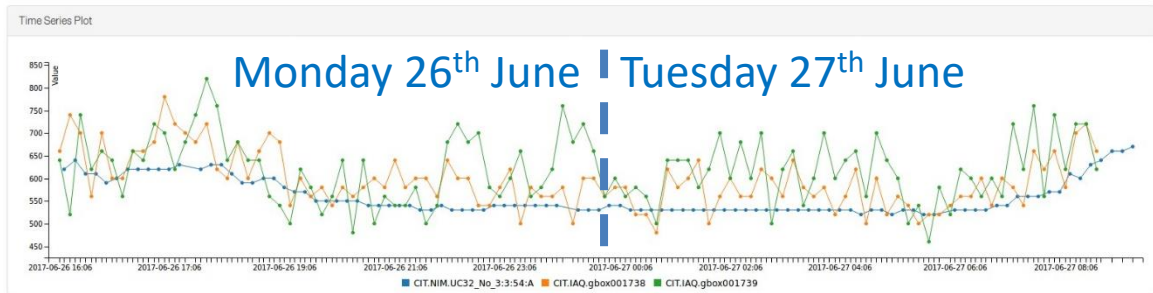
Full matrix

No more **physical meaning** for the parameters

- **Use directly identification techniques (Output Error + constraints)?**
 - directly estimate discrete-time state-space model
 - Take advantage of **knowledge from white-box model**
 - Multiple Inputs Single Output (MISO) models
 - Transfer functions ➔ state-space representation



- As for many industrial systems: **availability & reliability of data?**
 - **Data losses** (wireless, wired)
 - Data accuracy → e.g. #occupants
 - Noise
 - Synchronisation
 - Occupancy per zone
 - **Badge**
 - **Several persons**
 - **No information on the zone** → uniform distribution, periodic reset
 - Power delivered by heaters
 - Coarse estimation (inlet/outlet temperature for the **whole floor**)
 - Windows opening
 - **Manual** ones!
 - Controlled ones but also **partly non-functioning**



2 days of trustful
data record
→ Identification
→ Validation



- Model Inputs:

For zone 1

- [u]
- Windows opening per zone: w_1 (N.U.), w_2 (N.U.), w_3 (N.U.)
 - Heaters: P_1 (kW), P_2 (kW), P_3 (kW)
 - T_{out} (°C)
 - #occupants: Nb_1 (N.U.), Nb_2 (N.U.), Nb_3 (N.U.)

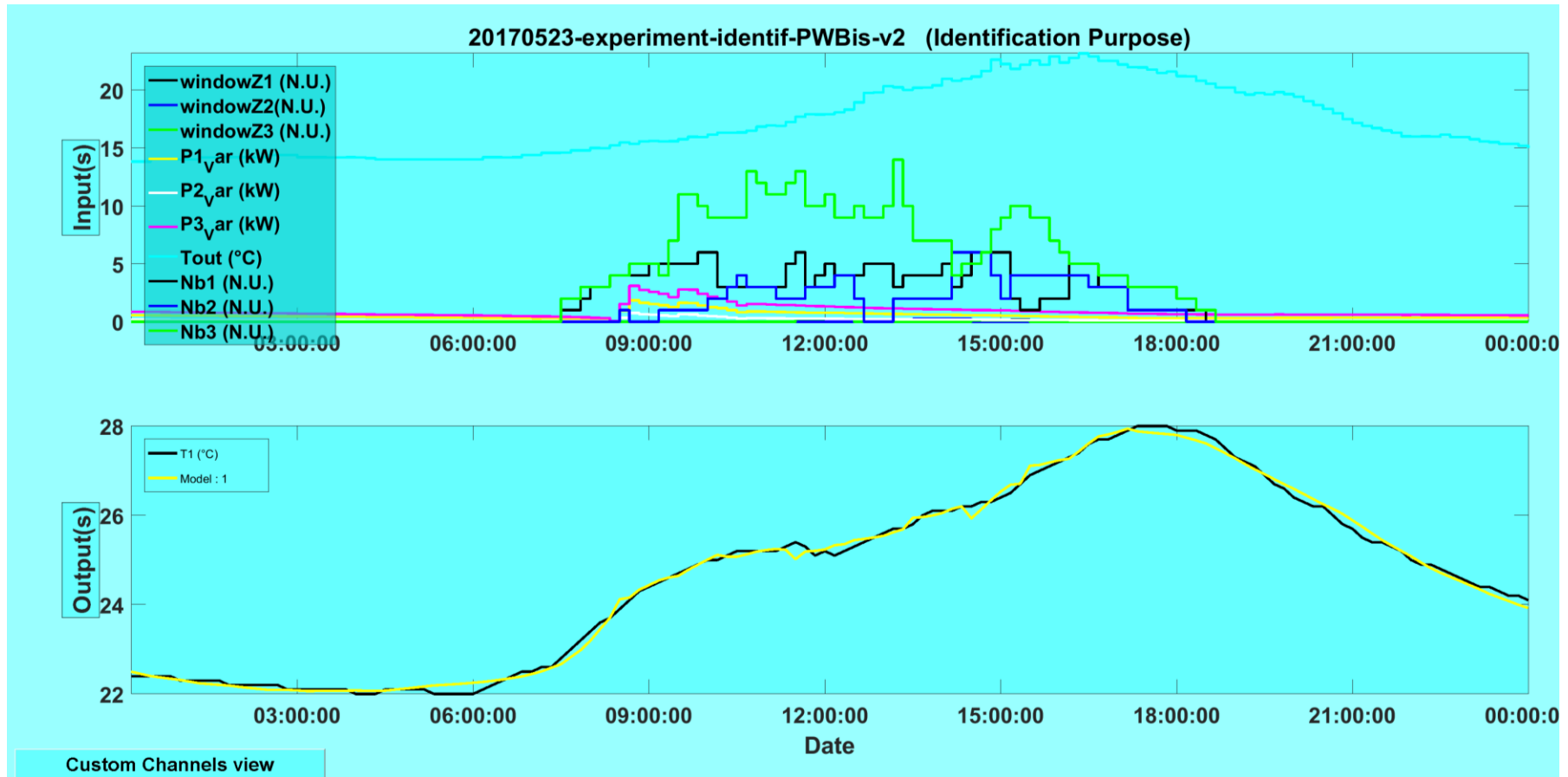
- Model Output: T_1 (°C) = y

$$[x]_{k+1} = [A][x]_k + \underbrace{B_1 \begin{bmatrix} w_1 \\ w_2 \\ w_3 \end{bmatrix} + B_2 \begin{bmatrix} P_1 \\ P_2 \\ P_3 \end{bmatrix}}_{\text{Control inputs}} + \underbrace{B_3 [T_{out}] + B_4 \begin{bmatrix} Nb_1 \\ Nb_2 \\ Nb_3 \end{bmatrix}}_{\text{Measured "disturbances"}}$$

$$T_1 = y_k = [1 \quad 1 \quad 1]x_k + D[u]_k$$



- **Model selection:** standard deviation, pole/zero simplification, goodness of fit ...



Model validation with another set of data



- Model Inputs:

For zone 1

- $[u]$
 - Nb1 (N.U.), Nb2 (N.U.), Nb3 (N.U.)
 - windowZ1 (N.U.), windowZ2(N.U.), windowZ3 (N.U.),

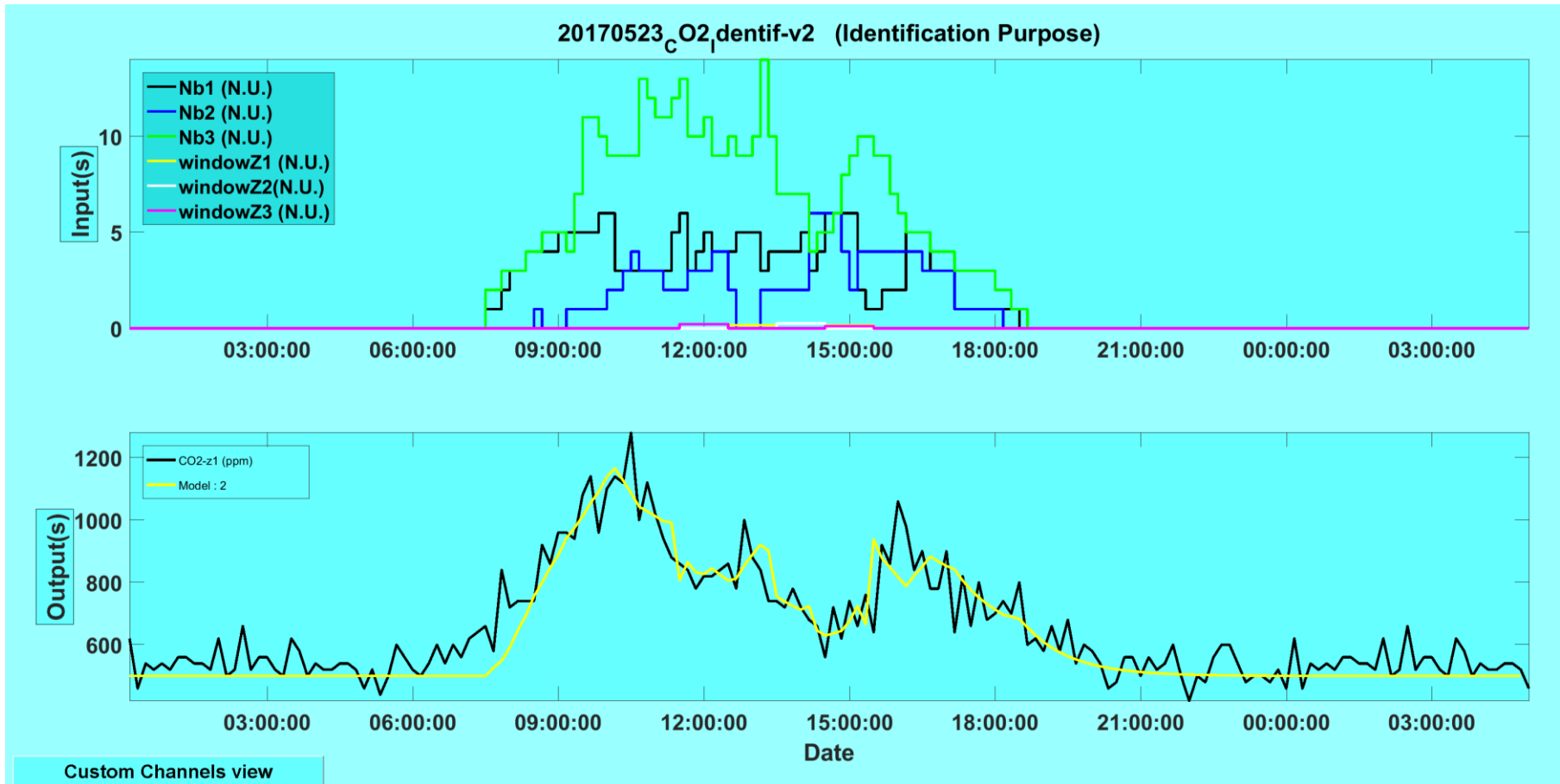
- Model Output: $CO2_{z2}$ (ppm) = y

$$[x]_{k+1} = [A][x]_k + B_1 \underbrace{\begin{bmatrix} Nb_1 \\ Nb_2 \\ Nb_3 \end{bmatrix}}_{\text{Measured "disturbances"}} + B_2 \underbrace{\begin{bmatrix} w_1 \\ w_2 \\ w_3 \end{bmatrix}}_{\text{Control inputs}}$$

$$CO2_{z1} = y_k = [1 \quad 0 \quad 0]x_k + D[u]_k$$



- **Model selection:** standard deviation, pole/zero simplification, goodness of fit ...



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Next steps

- Currently under implementation on NIMBUS
 - (D)MPC framework developed by CIT
 - through LINC middleware (M. Louvel, presentation on Wednesday)
- Model improvement
 - Take **solar** irradiance into account
 - Longer period of time for identification / validation
- TOPAs: “GAP reduction”
 - **Model re-adaptation** when the “gap” (prediction / measure) is too large